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# Agenda

- o Text data mining
- o Graph theoretic formulation
- o Text data mining preliminary results
- Graph theoretic formulation modified for gene expression data
- o Preliminary results on Golub data
  - Text data mining reenters the picture
- o Preliminary results on the Alon data





- What are we trying to do?
  - Develop new and extend existing methods of subspace/biclustering.
- What is our approach predicated on?
  - The synthesis of methodologies from statistics, mathematics and visualization.
- What are the test cases?
  - Roughly 1200 Science News abstracts that have been precategorized into 8 categories.
  - Roughly 343 Office of Naval Research In-house Laboratory Independent Research documents.
  - Golub gene expression data.
  - Alon concer data

# What is Biclustering and Subspace **Clustering**?

- o Given a set of n observations in p dimensions (an n by p matrix).
- o Biclustering is the simultaneous clustering of observations and dimensions.
- Subspace clustering is the identification of cluster structures that may be manifest only on a subset of dimensions.
  - The cluster structures may reside on manifolds or lower dimensional subspaces in the ambient space.

Getz G, Levine E, and Domany E. Coupled two-way clustering correct analysis of gene microarray datas" *Proc Natl Acad Sci USA* 97

# **Text Data Mining Applications**

- Literature based discovery
- o Formulation of research agendas
  - BAA announcements
  - Conference agendas
- Technology point papers
  - Discipline area
  - Country X

disease Y

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- Country X vs. Country Y
- Assessment of gene discoveries
  - Literature evidence relationship between gene G and GMU Bioinformatics Colloquium 2/15/05





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# **Document Features**

- o Bigram Proximity Matrices ala Martinez 2002
  - Angel Martinez, "A Framework for the Representation of Semantics," *Ph.D Dissertation under the direction of Edward Wegman*, October 2002.
- o Mutual Information Features ala Lin 2002
  - Patrick Pantel and Dekang Lin, "Discovery word senses from text," in Proceedings of the ACM SIGKDD Conference on Knowledge Discovery and Data Mining, pgs.
    - 613-619, 2002.

o "Normalized" term document matrices ala Dhillon 2001

- Inderjit S. Dhillon, "Co-clustering documents and words



### The Graph Theoretic Formulation

Adjacency Matrix

 $M \;=\; \left\{ egin{array}{cc} E_{ij}, & ext{ if there is an edge } \{i,j\}, \ 0, & ext{ otherwise.} \end{array} 
ight.$ 

The cut between two subsets of vertices.

$$\operatorname{cut}(\mathcal{V}_1, \mathcal{V}_2) = \sum_{i \in \mathcal{V}_1, j \in \mathcal{V}_2} M_{ij}$$

The cut between k subsets of vertices.  $\operatorname{cut}(\mathcal{V}_1, \mathcal{V}_2, \dots, \mathcal{V}_k) = \sum_{i < j} \operatorname{cut}(\mathcal{V}_i, \mathcal{V}_j)$ 





### The Document Word Bipartite Model

Our graph consisting of a vertex set consisting of documents and words along with associated edges.  $G = (\mathcal{D}, \mathcal{W}, E)$ 

The word vertices.  $\mathcal{W} = \{w_1, w_2, \dots, w_m\}$ 

The document vertices.  $\mathcal{D} = \{d_1, d_2, \dots, d_n\}$ One strategy for setting the edge weights.  $E_{ij} = t_{ij} \times \log\left(\frac{|\mathcal{D}|}{|\mathcal{D}_i|}\right)$ 

where  $t_{ij}$  is the number of times word  $w_i$  occurs in document  $d_j$ ,  $|\mathcal{D}| = n$  is the total number of documents and  $|\mathcal{D}_i|$  is the number of documents that contain word  $w_i$ .

$$M = \begin{bmatrix} 0 & A \\ A^T & 0 \end{bmatrix}$$
 Adjacency Matrix -  $A_{ij} = E_{ij}$ , 0's reflect no word to  
word or document to document connections  
 $\operatorname{cut}(\mathcal{W}_1 \cup \mathcal{D}_1, \mathcal{W}_2 \cup \mathcal{D}_2, \dots, \mathcal{W}_k \cup \mathcal{D}_k) = \min_{\mathcal{V}_1, \mathcal{V}_2, \dots, \mathcal{V}_k} \operatorname{cut}(\mathcal{V}_1, \mathcal{V}_2, \dots, \mathcal{V}_k)$   
Our Clustering  
Criteria

### Corpus Dependent Stop Word Removal

- Stop words are removed.
- Words occurring in less than 0.2% of the documents are removed.
- Words occurring in greater than 15% of the documents are removed.
- o N. B.

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- The methodology has been shown successful even if stopper words are not removed.
- 0.2% and 15% are user "tunable" parameters.







### The Left and Right Singular Vectors

$$\boldsymbol{A}_{\boldsymbol{n}}\boldsymbol{v}_{2} = \sigma_{2}\boldsymbol{u}_{2}, \qquad \boldsymbol{A}_{\boldsymbol{n}}^{T}\boldsymbol{u}_{2} = \sigma_{2}\boldsymbol{v}_{2},$$
  
$$\sigma_{2} = 1 - \lambda_{2} \qquad (4.12)$$

The right singular vector  $v_2$  will give us a bipartitioning of documents while the left singular vector  $u_2$  will give us a bipartitioning of the words. By examining the relations (4.12) it is clear that this solution agrees with our intuition that a partitioning of documents should induce a partitioning of words, while a partitioning of words should imply a partitioning of documents.

The curious fact is that the obtained transformation allows one to map the documents and words into the same onedimensional space.



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# Algorithm Multipartition(k)

$$Z = \begin{bmatrix} D_1^{-1/2}U \\ D_2^{-1/2}V \end{bmatrix} (4.14)$$

 $oldsymbol{U} = [oldsymbol{u}_2, oldsymbol{u}_3, \dots, oldsymbol{u}_{\ell+1}], \hspace{0.2cm} oldsymbol{u} = [oldsymbol{v}_2, oldsymbol{v}_3, \dots, oldsymbol{v}_{\ell+1}], \hspace{0.2cm} oldsymbol{\ell} = \lceil \log_2 k 
ceil$ 

Algorithm Multipartition(k)

- 1. Given  $A_n$ , form  $A_n = D_1^{-1/2} A D_2^{-1/2}$ .
- 2. Compute  $\ell = \lceil \log_2 k \rceil$  singular vectors of  $A_n$ ,  $u_2, u_3, \ldots u_{\ell+1}$  and  $v_2, v_3, \ldots v_{\ell+1}$ and form the matrix Z as in (4.14).
- 3. Run the k-means algorithm on the  $\ell$ -dimensional data Z to obtain the desired k-way multipartitioning.







# How Do We Know That the Dhillon 2001 Strategy is Worthwhile - II

o Confusion matrix performance on the

- Science News
- ONR ILIR Data
- Theoretical results that insure us that the spectral based approach is a good approximation to solving the NP-compete problem.







# Inherent Dimensionality of the Projected Data

o Multipartition

- Moderately low dimensional space log<sub>2</sub>(k)

o Recursive Bipartition

- Set of one-dimensional spaces

 Use minimal spanning trees to facilitate layout and exploration of the documents associated with each cluster.











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	Class1	Class2	Class3	Class4	Class5	Class6	Class7	Class8
Cluster1	0	0	3	0	9	0	208	0
Cluster2	2	0	5	32	77	4	91	20
Cluster3	0	0	0	0	0	0	0	3
Cluster4	1	19	0	89	18	2	0	5
Cluster5	1	25	0	6	5	12	3	95
Cluster6	7	0	75	1	8	43	7	9
Cluster7	37	0	5	36	57	4	1	12
Cluster8	0	80	0	0	0	0	0	0

### Science News 8 Multi-Partitioning Confusion Matrix

Class 1 is anthropology and archaeology, class 2 astronomy and space sciences, class 3 is behavior, class 4 is earth and environmental sciences, class 5 is life sciences, class 6 is mathematics and computers, class 7 is medical sciences, and class 8 is physical sciences and technology.

### Science News 8 Recursive Bi-partitioning

ANTHROPOLOGY & ARCHEOLOGY BEHAVIOR LIFE SCIENCES MEDICAL SCIENCES

ASTRONOMY & SPACE SCIENCES EARTH & ENVIRONMENTAL SCIENCES MATHEMATICS & COMPUTERS PHYSICAL SCIENCE & TECHNOLOGY



	Class1	Class2	Class3	Class4	Class5	Class6	Class7	Class8
Cluster1	19	0	55	1	10	29	2	9
Cluster2	25	0	3	69	79	0	10	9
Cluster3	2	20	0	(75)	10	2	0	13
Cluster4	1	0	29	8	57	3	263	4
Cluster5	0	0	0	8	13	0	33	11
Cluster6	0	102	0	3	0	1	0	9
Cluster7	0	0	0	0	0	(J3)	0	2
Cluster8	1	2	1	0	5	17	2	87

## Science News 8 Recursive-Bipartitioning Confusion Matrix

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# **Implementation Details**

- Developed software was implemented using Bioconductor and R
- o <a href="http://www.bioconductor.org/">http://www.bioconductor.org/</a>
- o <a href="http://lib.stat.cmu.edu/R/CRAN/">http://lib.stat.cmu.edu/R/CRAN/</a>



















### Golub Training & Test Data Sets

From the bipartitioning, 264 genes were grouped in the ALL cluster and 307 genes were grouped in the AML cluster

Using only the 264 genes and the 47 ALL samples, try to partition the B-cell and T-cell subclasses (results below)

B-cell class contains 189 genes

T-cell class contains to contains the contains and the contains a contain the contains a contains a contain the contains a contains

	B-cell	T-cell
S <sub>0</sub>	35	0
<b>S</b> <sub>1</sub>	3	9



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### Getz, Levine, and Domany 2000 Normalization Issue

This particular gene has been normalized by the paper's method. This method essentially mean centers each gene with sd=0.11.

The problem in applying the bipartition algorithm to genes that have been scaled this way is that it requires a SVD on the edgeweight matrix, such that this type of gene will stand out in the second singular vector from the SVD.

When one goes to then *k*-means cluster this 1-D vector, this gene will be assigned to its own cluster, since it's value far exceeds any other



# Golub Training & Test Data Sets

Using Paper's 1753 Genes and Our Original Edge Weight Scheme

# Bipartition method sample confusion matrix

	ALL	AML
S <sub>0</sub>	47	8
S <sub>1</sub>	0	17

Multipartition method sample confusion matrix

	B-cell	T-cell	AML
<b>S</b> <sub>0</sub>	22	3	0
<b>S</b> <sub>1</sub>	2	6	0
5 <sub>2</sub>	14	0	25



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# Golub Training & Test Data Sets

### Using Paper's 1753 Genes and Alternative Edge Weight Scheme

# Bipartition method sample confusion matrix

	ALL	AML
S <sub>0</sub>	28	1
S <sub>1</sub>	19	24

# Multipartition method sample confusion matrix

	B-cell	T-cell	AML
<b>S</b> <sub>0</sub>	27	5	7
<b>S</b> <sub>1</sub>	11	4	0
5 <sub>2</sub>	0	0	18











### Bipartitioning on AML Samples to Reveal Treatment

Bipartition on the 264 AML genes using only the 25 AML samples and Dr. Solka's edge-weight scheme performs as follows:

11/15 treated patients (CALGB) partition into group #1 (GLD paper has 14/15)

1 St-Jude patient partitions into group #1

1 CCG patient partitions into group #1

Concerned about confounding factor of hospital vs. treatment since all treated patients are stratified on same location

Genes from  $W_0$  and  $W_1$  have many related to DNA replication/repair and cellular growth/proliferation.

Similar to GLN 16 aene cluster in cellular





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