

Introduction to Bioinformatics

BINF 630

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Multiple Sequence Alignments

Multiple Sequence Alignment

```

Csp1_Hs  KTS DSTFLVFMSEGI RE-----G ICGKKHSEQVPDILQ-LNAIFNMLNT--3-PSLKD KPKV I I Q A C R G D-S P G V V W F
Csp2_Hs  RVT D S C I V A L L S E G V E-----G A I Y G V D G---K L L Q-L Q E V F Q L F D N--3- P S L Q N K P K M F F I Q A C R G D E T D R G V D Q
Csp3_Hs  S K R S S F V C V L L S E G E E-----G I I F G T N-----G P V D-L K K I T N F F R G--3- R S L T G K P K L F I I Q A C R G T E L D C G I E T
Csp9_Hs  G A L D C C V V V I L S E C C A S H L Q F P G A V Y G T D G---C P V S-V E K I V N I P N G--3- P S L G G K P K L F F I Q A C G G E Q K D H G F E V
Csp10_Hs A D G D C F V F C I L T E G R F-----G A V Y S S D E---A L I P-I R E I M S H P T A--3- P R L A E K P K L F F I Q A C G G E I Q P S V S I
CED3_Ce  G--D S A I L V I L S E G E E-----N V I I G V D D---I P I S-T H E I Y D L L N A--3- P R L A N K P K I V F V Q A C R G E R R D N G P P V

PC_Hs    D K G V Y G L L Y Y A G E G Y E N-----F G N S F M V P V D---A P N P Y R S E N C L C V Q N--5- Q E K E T G L N V F L L D M C R K R N D Y D D T I P
PC_Ce    G N G V Y A V F Y F V G E G F E V-----N G C Y L L G V D---A P A D A H Q P Q H S M S M D--6- R H K T P D L N L L L L D V C R K F V P Y D A I S A
PC_Dd    Q S Y I E V V V Y Y A G E G R S D-----N G N L K L I M T---D G N P V Q L S I I A S T L T--2- I K N S D S L C L F I V D C C R D G E N V L P F H Y
Mlr1804_M1 I G A D M A V F Y Y A G E A L Q Y-----N G Q N Y L-----L P V D T R I S S A K E V A A--12- K N D P V G V K V F I L D A C R N N P V A K E K G L
Mlr12372_M1 R G A D V A L F Y Y A G E G L Q V-----S G K N Y L-----L P V D A A L E D E T S L D F--11- M S R E T S I R L V F L D A C R D N P L A D V L A K
Mlr3463_M1 E G A G V G L F Y Y A G E G L Q V-----D G R N Y I-----V P V D A K L D M P V K L Q L--11- M E Q Q T K V S L V F L D A C R N N P F A R S L S R
Mlr15190_M1 K G A D V A L V Y F S G E G V E I-----S G D N R L-----L P V D A D A S S V D Q L D K--12- V A A T A K V G L I V L D A C R S D P F S A S S G D
Mlr1170_M1 E G A D V A F I Y Y S G E G I E A-----G G E N-----Y L V P V D A D V S S L K D A G Q--11- L K K T V P V T I M L L D A C R T N P F P A D A V V
YOR197w_Sc Q P N D S L F L H Y S G E G G Q T E D---L D G D E E D G M--D D V I Y P V D F E T Q G P I I D D E--8- P L Q Q G V R L T A L F D S C H S G T V L D L P Y T

MC1_At  T A G D S L V F H Y S G E G S R Q R N---Y N G D E V D G Y--D E T L C P L D F E T Q G M I V D D E--7- P L P H G V K L H S I I D A C H S G T V L D L P F L
MC2_At  K P G D S L V F H F S G E G N N Q M D---D N G D E V D G F--D E T L L P V D H R T S G V I V D D E--7- P L P Y G V K L H A I V D A C H S G T V M D L P Y L
MC3_At  K P G D V L V H Y S G E G T R L P A---E T G E D D D T G Y D E C I V P C D--M N L I T D D E F R--4- K V P K E A H I T I I S D S C H S G G L I D E A E
Mlr3300_M1 Q R D D F V Y L H L S G E G A Q Q P E R--A K G D E T D G L D E--I F L P V D I E K W I N R D A G V--15- I R N K G A F V W A V F D C C H S G T A T R A V E V
MCH_Rsph E P G G I F L M S Y A G E G A Q I G D F D E G D G P D R D R L D E T L C L H D--A M L V--D D E L Y--4- A F R E G V R V V A V F D C C H S G S I L R A S A N
MCH_Gsul G K G D I F M L S Y S G E G G Q V P---D T G N D E P D G V D E T W C L F D--G E L I--D D E L Y--4- K F A A G V R V L V F S D S C H S G T V V K M A Y Y

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Figure: Conserved catalytic motifs in the caspase-like superfamily of proteases.

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Knowledge gain

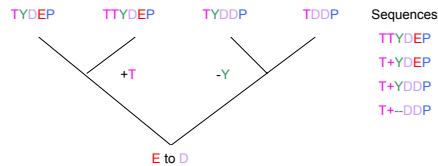
- *In science, “knowledge” is in the patterns/similarities. The interesting questions, however, are in the differences.*

Multiple Sequence Alignment

- It is believed, based on finding similar protein sequences within highly divergent species, that the over time the functional components embedded within the sequences are conserved in order to retain the function.
 - One of the most important elements of sequences is the phylogenetic information that similarities represent.
 - The sequence similarities gives insight into the evolution of families of protein or DNA sequences.
 - Knowledge to be gained:
 - Estimation of evolutionary distance
 - Mutation / Speciation
 - *Note: Multiple Sequence Alignment methods are also employed in assembly of DNA sequences from cloning vectors.*

Multiple Sequence Alignment

- Evolutionary distance:



- Phylogenetic distance is a measure of divergence between two similar sequences.
 - It can be thought of as the number of changes/ substitutions that have occurred, or the number of differences.
 - The simplest estimation of distance is to count the number of base mismatches m between the two sequences when aligned, then present this value as a proportion, or percentage, of the total alignment length n .
$$D = m/n \quad (1)$$
 - Including gaps and indels...
$$D = m/(n - g) + [g * \text{penalty}] \quad (2)$$
Where g is the total number of gaps within the alignment's consensus sequence.

Multiple Sequence Alignment Methods

- Global alignment:

- Homologous proteins
 - Structural similarity → Functional similarity
 - Common evolutionary origin

- Local alignment:

- Conserved regions
 - Structural motif → Functional domains
 - Phylogenetic or ancestral similarity

Multiple Sequence Alignment Methods

- **Global Alignment Tools:**
 - **Dynamic Programming Based**
 - MSA [1]
 - ClustalW Thompson et al. (1997) [1]
 - **Iterative Methods**
 - Simulated Annealing
 - MSASA
 - Genetic Algorithm
 - SAGA and RAGA
 - **Local alignment tools:**
 - **Gibbs based**
 - GIBBS Lawrence (1993) BLOCKS Henikoff and Henikoff(1992) [1]
 - **Hidden Markov Model**
 - HMMER (Eddy 1998)
 - **EM based**
 - MEME Bailey and Elkan (1995)
- [1] <http://searchlauncher.bcm.tmc.edu/multi-align/multi-align.html>
[2] <http://bayesweb.wadsworth.org/gibbs/gibbs.html>

Global: Multiple Sequence Alignment

- **MSA (Multiple Sequence Alignment):**
 - Based on dynamic programming
 - Aligns two sequences
 - Provides a measure of accuracy of alignments
 - Scores the alignment – level of significance
 - Different applications can handle *indels* as well as *gaps*.
 - Depends on choice of scoring system
 - Results change based on the scoring matrix
 - PAM : Evolutionary change
 - BLOSUM : Family membership
 - Different types of gap penalties
 - Affine gap
 - Most methods employ a phylogenetic tree building to concatenate alignments.

Sequence Alignment Review

- Dynamic Programming

- Global

- Needleman-Wunsch

$$D_{0,0} = 0$$

$$D_{0,j} = \sum_{k=1}^j w(-, b_k)$$

$$D_{i,0} = \sum_{k=1}^i w(a_k, -)$$

$$\forall i, j > 0 \quad D_{i,j} = \min \left\{ \begin{array}{l} D_{i,j-1} + w(-, b_j) \\ D_{i-1,j-1} + w(a_i, b_j) \\ D_{i-1,j} + w(a_i, -) \end{array} \right\}$$

where w is the weight of a gap

- Local

- Waterman-Smith-Beyer

$$D_{0,0} = 0$$

$$D_{0,j} = g(j)$$

$$D_{i,0} = g(i)$$

$$\forall i, j > 0 \quad S_{i,j} = \min \left\{ \begin{array}{l} \min_{1 \leq k \leq j} (D_{i,j-k} + g(k)) \\ D_{i-1,j-1} + w(a_i, b_j) \\ \min_{1 \leq k \leq j} (D_{i-k,j} + g(k)) \end{array} \right\}$$

where $g(k)$ is the gap penalty function and w is the similarity score function

Multiple Sequence Alignment – Dynamic Programming

- An extension of the pair wise sequence alignment
 - Alignment of k sequences to k sequences
 - $k(k-1)/2$ possible sequence comparisons.

- Alignment algorithms operate in a similar manner as before but now the distance matrix is (k dimensional) and the weight function compares k letters.
 - 2D – simple matrix
 - 3D – Hypercube
 - kD – k dimensional hyperspace

MSA: Dynamic Programming

- Assume that we are trying to align three sequence a,b, and c.
- Also assume that we have a cost function $w(x,y,z)$ that computes the cost of comparing x, y, and z in sequences a, b, and c respectively.

$$w(x, y, z) = \begin{cases} 0 & x = y = z \\ 1 & \text{2 of 3 symbols are the same} \\ 2 & x \neq y \neq z \end{cases}$$

MSA: Dynamic Programming

Then our distance matrix D can be described by:

$$\forall i, j, k > 0 \quad D_{i,j,k} = \min \left\{ \begin{array}{l} D_{i-1,j-1,k-1} + w(a_i, b_j, c_k) \\ D_{i,j-1,k-1} + w(-, b_j, c_k) \\ D_{i-1,j,k-1} + w(a_i, -, c_k) \\ D_{i-1,j-1,k} + w(a_i, b_j, -) \\ D_{i-1,j,k} + w(a_i, -, -) \\ D_{i,j-1,k} + w(-, b_j, -) \\ D_{i,j,k-1} + w(-, -, c_k) \end{array} \right\}$$

MSA: Dynamic Programming

- Computationally expensive
 - Long sequences
 - Large number of sequences
- Computational cost
 - For two sequences of lengths n and m
 - Needleman-Wunsch
 - $O(nm) = O(n^2)$ for $n \geq m$
 - Waterman-Smith-Beyer
 - $O(nm(n+m)) = O(n^3)$ for $n \geq m$
 - Gotoh's algorithm
 - $O(nm) = O(n^2)$ for $n \geq m$
 - For three sequences of lengths n , m and p
 - Most algorithms
 - $O(nmp) = O(n^3)$ for $n \geq m \geq p$

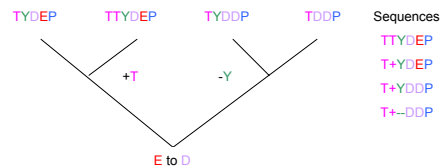
MSA: Dynamic Programming

- For k sequences we get $O(n^k)$ where n is the longest sequence
 - If we compare 10 sequences of length ≤ 300
 - 300^{10} comparisons....
 - 5,904,900,000,000,000,000,000,000
 - np-complete task

Global Alignment: Dynamic Programming

■ Solutions:

- Sum of Pairs *Carrillo and Lipman (1988)*
 - Look at all pairs
 - Create parsimony tree
 - Build alignment along the tree
 - Take the best SP score
 - Problems:
 - Biased toward similar sets of sequences.
 - Order weighting important



Global Alignment: Dynamic Programming

■ Progressive Methods

- Dynamic Sequence alignment based on hierarchical sequence similarity.
- Challenge:
 - To choose the correct
 - Sequence weighting
 - Scoring matrix
 - Gap penalties
- Goal get the correct series of evolutionary changes
- Programs:
 - CLUSTALW
 - Gaps between conserved regions down weighted
 - Already occurring gaps down weighted
 - New Gaps are costly
 - T-Coffee
 - Employs locally aligned (conserved regions/domains) to help find alignment

Global MSA: Genetic Algorithms

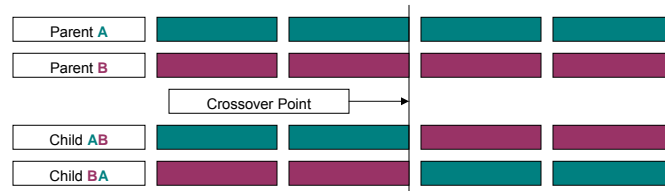
- SAGA Notredame and Higgins (1996)
 - Basic steps
 - 1) Pair wise global alignment
 - 2) Phylogentic tree
 - 3) Weight sequences
 - 4) Iterative refinement of MSA via GA
 - Check score and if not good enough return to 2

Global MSA: Genetic Algorithms

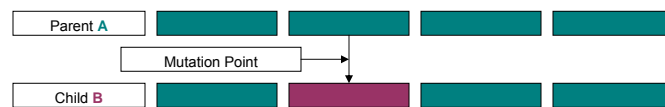
- GA developed by computers scientists as a machine learning application.
- Typical GA flow:
 - Initialize the study population
 - Evaluate the population
 - while (not termination condition)
 - Alter the population at this step
 - Reproduction – combination of members
 - Mutation – random changes in the population
 - Crossover – moving information between members
 - Re-evaluate the population
- Departmental expert
 - Dr. John Grefenstette

Crossover and Mutation

Crossover



Mutation



Global MSA: Other methods... and what works best.

- Simulated Annealing
 - Pair-wise alignment driven
 - Heuristic algorithm to iterate and improve the score
 - MSASA (Kim et al. 1994)
- Graph based methods
 - Directed acyclic graphs
 - Partial order graphs
- Best??? (Lassman and Sonnhammer 2002)
 - DIALIGN (Best for low sequence identity)
 - T-COFFEE (Best for high sequence similarity)

Local MSA

- Small Conserved regions
 - DNA sequence → regulatory or coding region in DNA
 - Protein → functional domains
- The small regions are considered motifs or profiles
 - Regular Expressions
 - PSSM (position specific scoring matrix)
 - HMM (allows gaps and indels)
- Three main methods:
 - Profile analysis
 - Uses Conserved Regions of Global MSA
 - Uses the conserved regions to build a profile.
 - Block analysis
 - Looks for regions in an Global MSA with no substitutions
 - MOTIF then MOTOMAT
 - Uses these regions for alignments
 - Statistical and Pattern searching methods
 - HMM
 - EM
 - Gibbs

Local MSA: Sequence patterns

```
KKFAQSTNLKSHILT
KQFSHSAQLRAHIST
GKFSDSNQLKSHMLV
KDISSSESLRTHMFK
KRFSHSGSYSSHISS
KRFSHSGSFSSHMTS
KTLSDRLEYQQHMLK
```

Local MSA: Protein Motif Databases

- PROSITE <http://www.expasy.org/prosite/>
 - Method:
 - CLUSTAL MSA based
- BLOCKS <http://blocks.fhcrc.org/>
 - Method:
 - MSA based
- PFAM <http://www.sanger.ac.uk/Software/Pfam/>
 - Method:
 - MSA and HMM models of protein motifs

Local MSA: PROSITE

- PROSITE
 - Current version contains
 - 1446 documentation entries that describe
 - 1331 patterns
 - 4 rules
 - 650 profiles/matrices
 - Cytochrome P450 cysteine heme-iron ligand signature
 - [FW] - [SGNH] - x - [GD] - {F} - [RKHPT] - {P} - C - [LIVMFAP] - [GAD]
 - *C is the heme iron ligand*

Regular Expressions

Patterns described in a standard way are known as *regular expressions*

x	ANY		
[]	OR	[ILV]	I or L or V
{ }	NOT	{DE}	not D or E
()	repetitions	x(2,3)	x-x or x-x-x
-	separator		
<	N-terminal		
>	C-terminal		
.	END		

Regular Expressions

[AC]-x-V-x(4)-{ED}

[Ala or Cys]-any-Val-any-any-any-any-{any but Glu or Asp}

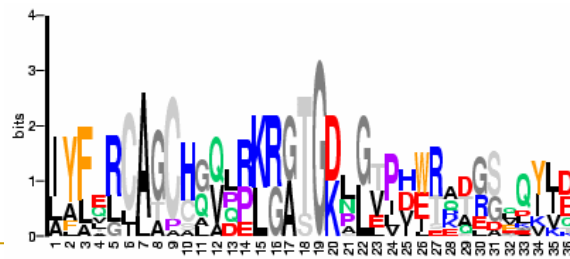
... LKHV**AYVFQALI**YWIK ...
... AVEM**AGVKYLQV**QHGS ...
... LYTG**AIVTNDG**PYMA ...
... KEYK**CKVEKELT**DICN ...

BLOCKS

- Blocks are multiply aligned un-gapped segments corresponding to the most highly conserved regions of proteins

- Block IPB003143A**

```
ID D1_heme; BLOCK AC IPB003143A; distance from previous block=(7,88)
DE Cytochrome d1, heme region BL ACG; width=36; seqs=12; 99.5%=1578; strength=1225
NIRF_PSEAE|Q51480 ( 9) LLTLLAGCSQQPPLRGSGLGVLIERADGSVQILD 59
NIRS_PARDE|Q51700 ( 89) IYFRCAGCHGVLRKGATGKALTPDLTRDLGFDYLQ 32
NIRS_PSEAE|P24474 ( 67) IYFRCAGCHGVLRKGATGKPLTPDITQRRGQYILE 29
NIRF_PSEST|Q52521 ( 8) LAAVGLLTACAQQPLRGTGDLGVVVERATGSLQIE 88
NIRS_PARFN|P72181 ( 89) IYFRCAGCHGVLRKGATGKALTPDLTRDLGFDYLQ 32
NIRS_PSEST|P24040 ( 42) IYFRCAGCHGVLRKGATGKLEPHWSKTEADGKKT 51
Q9R9J9 ( 8) AALLLIAPALADELRGTGDLGLIVERAGSLLVVD 100
Q44012 ( 53) IYFRCAGCHGVLRKGATGKSLTPDITRARGTEYLK 36
Q9F0W9 ( 58) IYFRCAGCHGVLRKGATGKPLTPDITQSRGQAYLE 32
```



PSSM of IPB003143A (D1_heme); 12 sequences.

Profile Method of Local MSA

- Two types of profile method
 - Weighted
 - Strictly drawn from Dayhoff PAM matrices based on amino acid frequency
 - Evolutionary
 - Rate of evolution is taken into account
 - Probability of the change between residues
 - Calculated as a log odds score of the Dayhoff method
 - The method for computation of the

Local MSA: Profile methods

- Standard method of Profile creation
 - Get a global alignment
 - Shorter highly conserved regions
 - Create a Profile matrix of the conserved region

- A profile is a scoring matrix
 - Row for each residue in the Profile
 - 23 columns
 - 20 : each amino acid
 - 1 : unknown residue z
 - 2 : Gap and extension

 - These scores are based on strict counts

Local MSA: Profile methods

- BLOCKS
 - Short highly conserved regions
 - Can be 3-60 amino acids in length
 - Typically 10 – 55

 - Do not contain gaps

 - Are typically calculated by strict counts
 - Do not typically account for or include evolutionary measures.
 - Are good for pattern searching

 - Cons:
 - Limitation to length
 - Only as good as the MSA that they are built with

 - MOTIF always finds a BLOCK even in random sequences

Local MSA: Statistical Methods

- EM (Expectation Maximization)
 - Initial guess is made as to the location of a motif
 - Expectation Step
 - The probability of finding the motif at any any point in each of the sequences is calculated based on the distribution of bases/amino acids within each column of the initial guess.
 - The probabilities are used to redefine the initial distribution within each motif column.
 - Maximization Step
 - The new counts based on the probabilities are used to change the initial guess.
 - This is iterated until convergence
 - The size of a motif region can be determined by the EM algorithm based on log likelihood scores after one iteration

- GIBBS Sampler Method
 - Searches for the statistically most probable motifs.
 - The goal is to maximize the ratio of motif probability to background probability.

Hidden Markov Models: Local MSA

- Hidden Markov Models
 - Statistically based
 - Produce sound results

 - Provide representations of sequence domains or protein families

 - Drawback ...
 - Require lots of data to train...

Markov Chains



- Probability for each state
 - is based only on a set **number** of preceding characters
- # of preceding characters = **order** of the Markov Model
- Probability of a sequence (order = 2):
 - $P(s) = P\{T\} P\{T,C\} P\{T,C,A\} P\{C,A,G\} P\{A,G,C\} P\{G,C,C\} P\{C,C,T\}$

Hidden Markov Models



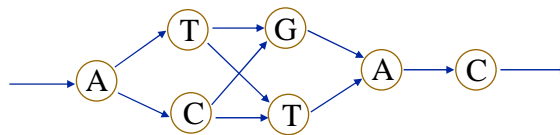
Observed	A	0.7	A	0.1	C	0.8	A	0.4	A	0.8	C	0.3
frequencies	T	0.3	T	0.9	G	0.2	T	0.6	T	0.2	G	0.7

Probabilistic model - true state is unknown

Hidden Markov Models

States -- well defined conditions

Edges -- transitions between the states



ATGAC
ATTAC
ACGAC
ACTAC

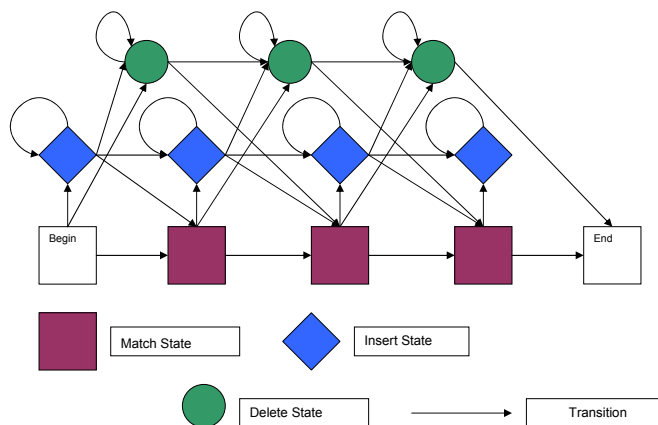
Each transition assigned a probability.

Probability of the sequence:

single path with the highest probability --- *Viterbi* path

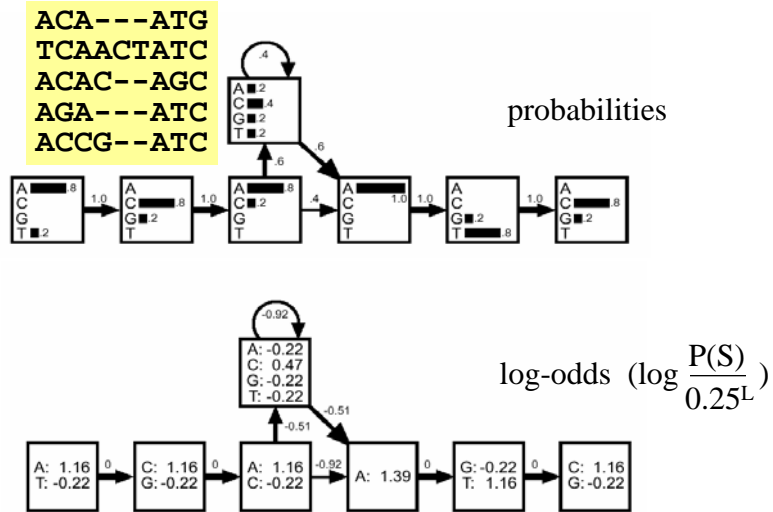
sum of the probabilities over all paths -- *Baum-Welch* method

Common Protein Sequence HMM



Adapted representation of the model by of Krogh et al. 1994

Hidden Markov Models



How HMMs are built/ trained

- Start with a basic model structure and a given distribution of probabilities
- Algorithms for training markov models
 - Forward and Backward Algorithms
- Predictive Measures
 - Viterbi
 - Baum-Welch
- Best practices to improve HMM performance
 - Alter prior distribution of amino acids
 - Knowledge added start point can emphasize convergence
 - Alter architecture based on familial knowledge

PSSM Calculation...

- The goal of local MSA is to find small regions that are highly conserved.
 - Once these regions are found it is important to consider the underlying distribution by which the motif was created.
 - What manner is the sequence to be compared
 - [FW] - [SGNH] - x - [GD] - {F} - [RKHPT] - {P} - C - [LIVMFAP] - [GAD]
 - Does this contain sufficient variation?
 - Most likely the search will be done with dynamic programming
 - Thus the scoring matrix is important and must contain sufficient variation, but at the same time limit the number of false predictions.
 - To do this we measure the scoring matrix how?
 - Shannon Entropy measure:

$$H(x) = - \sum_{i=1}^M P_i \log_2 P_i$$

- In this case the x is the column in the motif and i is the amino acid/base. P_i is the frequency of the amino acid/base.
- Total score for a scoring matrix can be the sum of all the column scores: $H_{total} = \sum H(x)$

The Logo Display of Shannon Entropy Scores for heme BLOCK.



PSSM of IPB0031.43A (D1_heme); 12 sequences.

In class exercise

- Get the file of protein sequences from my website
 - <http://binf.gmu.edu/dcarri/>
 - FATSAs_ProteinList.txt
- Get a global alignment
 - Does everything align?
 - What are the scores?
 - Do you see a motif?
- Remove 1AK0 and 1AKO
 - Why are we removing these two?
 - Get the alignment
 - What changes do you see?
 - Do you see a motif?
- Remove 1FY9
 - Why are we removing this protein?
 - Get the global alignment
 - What changes do you see?
 - Do you see a motif?
- What is 1DYP's function?
- What is 1GBG's function?
- Are these two proteins structurally similar?
- Do these two proteins have a similar functional site?
 - Where is the difference in the proteins? i.e. what provides the specificity.
- Get a local alignment (find a profile or motif for the sequences)
 - **What is the the regular expression of the motif region for this set of proteins?**
 - **Get the BLOCK motif for this region**
 - **What is the difference between the regular expression and the BLOCK?**
 - **What effect does this difference have?**